

## The Link Between Non-Thermal Velocity and Free Magnetic Energy in Solar Flares

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### ABSTRACT

The cause of excess spectral line broadening (non-thermal velocity) is not definitively known, but given its rise before and during flaring, the causal processes hold clues to understanding the triggers for the onset of reconnection and the release of free magnetic energy from the coronal magnetic field. A comparison of data during a 9-hour period from the extreme ultraviolet (EUV) Imaging Spectrometer (EIS) on the Hinode spacecraft - at a 3-minute cadence - and non-linear force-free field (NLFFF) extrapolations performed on Helioseismic and Magnetic Imager (HMI) magnetograms - at a 12-minute cadence - shows an inverse relationship between non-thermal velocity and free magnetic energy on short timescales during two X-class solar flares on 6 September 2017. Analysis of these results supports suggestions that unresolved Doppler flows do not solely cause non-thermal broadening and instead other mechanisms like Alfvén wave propagation and isotropic turbulence have a greater influence.

*Keywords:* Non-thermal velocity — Free magnetic energy — Non-linear force-free extrapolation — Extreme ultraviolet spectroscopy

### 1. INTRODUCTION

Solar flares are widely believed to occur as the result of the sudden and impulsive release of energy stored in non-potential magnetic fields (Toriumi & Wang 2019; Priest & Forbes 2002). These fields, rather than following the lowest energy configuration, exhibit a degree of twist or shear. The energy difference between these non-potential, i.e. current-carrying fields and their lowest energy state represents the energy stored in the magnetic field. It is known as free magnetic energy and is available to produce flares and coronal mass ejections (CMEs) (Wiegmann & Sakurai 2021). When a non-potential field transitions to a lower energy state through magnetic reconnection, the stored energy is released into

the solar atmosphere. This process, in line with the standard flare model (Shibata & Magara 2011), leads to plasma heating and particle acceleration (Pontin & Priest 2022; Fletcher et al. 2011; Benz 2017), serving as the fundamental mechanism for energy release in solar flares and the ejection of material in CMEs.

The creation of non-potential fields is primarily attributed to the emergence of magnetic flux - the ascent of twisted and distorted bundles of magnetic field lines through the solar convective zone, culminating in their emergence through the photosphere as twisted flux tubes - and their interaction with pre-existing fields (Leka et al. 1996). Other contributing factors include the shearing and twisting of the magnetic structures at the photosphere, for instance, the movement of footpoints (Park et al. 2018).

The non-thermal broadening of extreme ultraviolet (EUV) and soft X-ray lines has been observed to in-

crease substantially during flaring - reaching velocities as high as  $200 \text{ km s}^{-1}$  (e.g., [Doschek et al. 1980](#)) - and before flare onset, often showing enhancements tens of minutes prior to the start of the flare impulsive phase, (e.g., [Harra et al. 2001](#)). However, the precise relationship between the flare energy release processes and the origin of the excess line broadening remains unclear.

Active region NOAA 12673 has been the focus of significant attention in the solar community due to the notably energetic solar events it generated. First observed on the eastern solar limb on 31 August 2017, this region underwent substantial flux emergence starting on 3 September 2017. This rapid evolution precipitated the production of several M- and X-class flares, CMEs, and solar energetic particle (SEP) events (e.g., [Yan et al. 2018](#); [Verma 2018](#)). X-class flares, being the most energetic, are the class of flare most clearly reflected in both the free magnetic energy and non-thermal velocity, and are therefore ideal to use to study the relationship between these parameters.

Our study focuses on active region NOAA 12673 during the time period from 06:00 to 14:48 UTC on 6 September 2017, an approximately 9-hour window that saw a confined X2.2 flare and an eruptive X9.3 flare (e.g., [Gupta et al. 2021](#); [Hou et al. 2018](#); [Mitra et al. 2018](#)). We undertook a comprehensive analysis of the free magnetic energy release in the active region during this interval, exploring its correlation with non-thermal velocity for multiple EUV emission lines. In this paper, we study the corona's response to the non-potential field configuration, particularly with respect to the coronal emission line widths, and quantify this relationship.

## 2. OBSERVATIONS AND EXTRAPOLATIONS

This study combines data taken by the EUV Imaging Spectrometer (EUV) onboard the Hinode spacecraft ([Kosugi et al. 2007](#)) with photospheric magnetograms from the Helioseismic and Magnetic Imager (HMI) on board the Solar Dynamics Observatory (SDO). We additionally use the Geostationary Operational Environmental Satellite (GOES) system, specifically data from the X-ray Sensor (XRS) of the GOES-13 spacecraft.

### 2.1. EUV Observations

The EUV data used in this study were gathered between 06:20 and 14:50 UTC on 6 September 2017 by EIS. The EIS instrument is a scanning slit spectrometer that observes the solar corona and upper transition region in two EUV wavebands: 170 Å to 211 Å and 246 Å to 292 Å ([Culhane et al. 2007](#); [Young et al. 2007](#)).

We analysed a series of raster scans taken during the observation period while EIS was operating a high-

cadence, reduced field-of-view flare study (study 473<sup>1</sup>) to capture the response of the coronal plasma to a flare. This study completes repeated scanning rasters, each with 30 pointing positions taken sequentially from west to east and with a scan step size of 4 arcsec. The exposure time for each pointing position was approximately 4 seconds which, when considering other instrumental operations, results in a raster cadence of approximately 3 minutes. The time given for each observation henceforth refers to the midpoint of the observation. There are a number of emission lines observed in this configuration ranging from cool to flaring lines. We focused on the strong Fe XIV 264.79 Å and Fe XIV 274.20 Å ( $\log T_{\text{max}} = 6.3$ ) coronal lines given they demonstrated a high signal/noise during both X-class flares, did not saturate during the peak intensities during flaring, and allowed consistently good fits throughout the detector and throughout the time series. The former is recommended for probing hotter parts of active regions, and so can be expected to react quickly to flaring activity. It is also not overlapped by any other known emission lines. The latter is blended with a small contribution from Si VII 275.35 Å which can be safely neglected ([Young et al. 2007](#)). These two lines were used in tandem, with the latter used to verify the response of the former, and indeed in our study, they both demonstrate very similar results. The strong Ca XVII 192.82 Å ( $\log T_{\text{max}} = 6.7$ ) flaring line was also used given its more specific response to flares, but required special additional consideration as is discussed later.

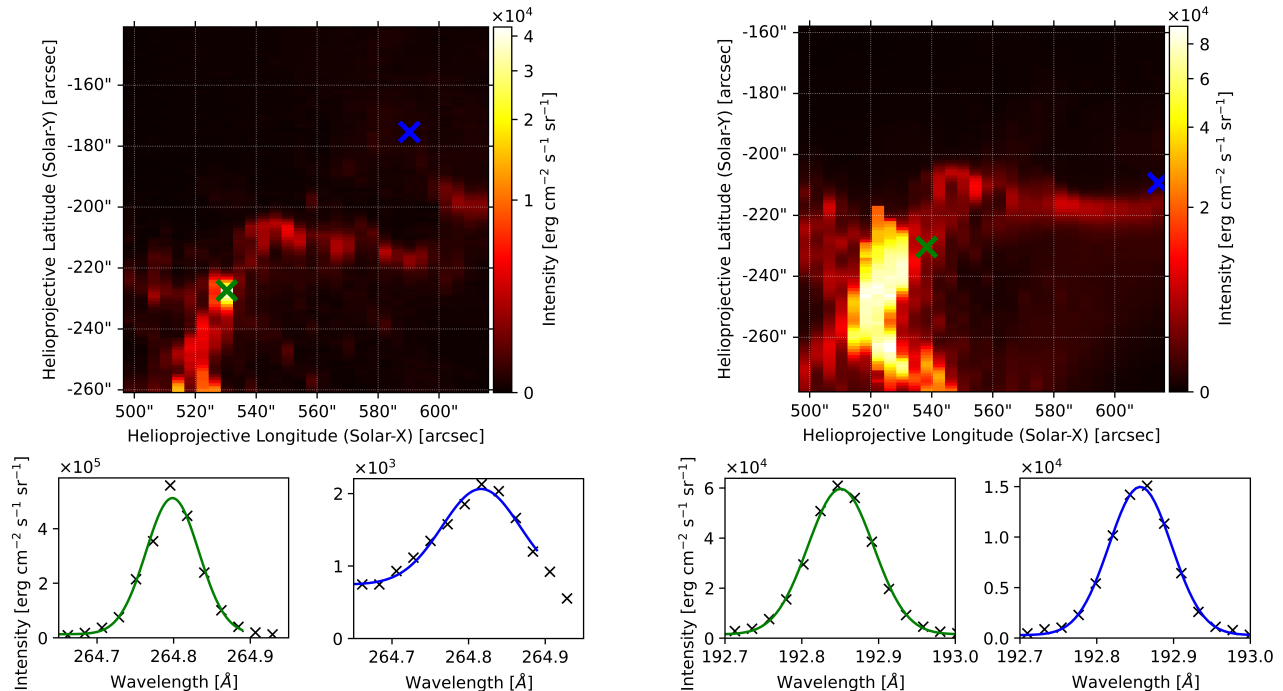
Gaussian fits were carried out for these lines, for each pixel in each raster scan using the EIS Python Analysis Code (EISPAC). An example of this fitting can be seen in [Figure 1](#). This fitting procedure results in maps of the line width which were converted into non-thermal velocity ( $v_{nt}$ ) using

$$\text{FWHM}_o^2 = \text{FWHM}_i^2 + 4 \ln 2 \left( \frac{\lambda}{c} \right)^2 (v_t^2 + v_{nt}^2), \quad (1)$$

where  $\text{FWHM}_o$  and  $\text{FWHM}_i$  refer to the observed and instrumental full width at half maximum values respectively, and where  $\lambda$ ,  $v_t$  and  $c$  refer to the central wavelength of the fitted Gaussian, the associated thermal velocity, and the speed of light.

The uncertainty in the instrumental width can be combined with the statistical error in the fitted Gaussian - partly caused by uncertainty in the measurement of each point in the emission line - using standard error

<sup>1</sup> <https://solarb.mssl.ucl.ac.uk/SolarB/>



(a) Fe XIV 264.79 Å intensity map and sample fitted spectra for the highest intensity (green) and median intensity (blue) pixels.

(b) Ca XVII 192.82 Å intensity map and sample fitted spectra for the 85% intensity (green) and median intensity (blue) pixels. Details on the saturation of some pixels are in the text.

**Figure 1.** Intensity map and sample fitted spectra for active region NOAA 12673, using data from Hinode/EIS at 11:58 UTC on 6 September 2017 during the onset of the X9.3 flare.

propagation (e.g., Bevington & Robinson 2003) to estimate the error in non-thermal velocity measurements to be approximately 25%.

The values for non-thermal velocity as observed by each pixel in the image, such as shown in Figure 1, were then averaged for each observation to generate one non-thermal velocity value for each observation time, resulting in a time series. This was found to be the most effective way to include a sufficient sample size in each observation to reduce noise, while still clearly capturing increases in non-thermal velocity.

As aforementioned, Ca XVII 192.82 Å requires careful consideration given it is part of a complex blend comprising seven other known lines. During low periods of activity, various methods can be used to estimate their respective contributions and isolate the Ca XVII emission. However, during flaring Ca XVII completely dominates and so any other contributions can be considered negligible (Young et al. 2007; Ko et al. 2009). Additionally, several wavelength bins within some pixels became saturated during both X-class flares in this study (at  $5 \times 10^5 \text{ erg cm}^{-2} \text{ s}^{-1} \text{ sr}^{-1}$ ). It was determined that the best approach to address this was to exclude any pixels within which any of the wavelength bins had become saturated, these accounting for only 1% of

Ca XVII 192.82 Å pixels in the complete dataset and peaking at approximately 10% of the Ca XVII 192.82 Å pixels in one observation during the X9.3 flare. This processing means that the Ca XVII 192.82 Å non-thermal velocity values should be considered a lower estimate.

The pointing information of the EIS data was corrected by co-aligning the Fe XIV 264.79 Å intensity maps with imaging performed at 171 Å by the Atmospheric Imaging Assembly (AIA) onboard SDO. This required only small longitudinal corrections, increasing due to drift during the 9-hour period to just less than 10 arcsec by the end of the observation.

## 2.2. Magnetic field observations

In addition to the EIS data we also used data gathered by HMI between 06:00 and 14:48 UTC on 6 September 2017, excluding a data gap between 06:12 and 08:24 UTC inclusive due to instrument downtime. The HMI instrument generates full-disk vector photospheric magnetograms with a cadence of 12 minutes and at a resolution of about 1 arcsec, with a noise level of about 100 G (Hoeksema et al. 2014).

For this study, we used the HMI vector magnetograms to perform non-linear force-free field (NLFFF) extrapolations of the photospheric magnetic field to then subse-

quently calculate the free magnetic energy of the magnetic field. The magnetograms used were those provided by Space-weather HMI Active Region Patches (SHARPs) in cylindrical equal area (CEA) projection, using SHARP 7115.

Based on the photospheric magnetic field, we performed a magnetic field extrapolation using the method developed by Jarolim et al. (2023), allowing for the production of a maximum cadence time series based on magnetograms with high spatial resolution. Here, a physics-informed neural network (PINN) is used to solve the force-free equation

$$J \times B = 0 \quad (2)$$

and divergence-free equation

$$\nabla \cdot B = 0, \quad (3)$$

where  $J$  is the electric current density and  $B$  is the magnetic field, for the given boundary condition. We compute the magnetic field  $B$  up to a height of approximately 115 Mm with re-binned magnetograms to 1/2 resolution, resulting in  $0.72 \text{ Mm pix}^{-1}$ .

Modelled field lines were validated against EUV emission structures imaged using AIA. Figure 2 shows low-lying loops in the sheared core of the active region are well matched to structures seen in AIA  $171 \text{ \AA}$ .

The total magnetic energy within the simulation volume  $V$  can then be calculated using

$$E = \int_V \frac{B^2}{8\pi} dV. \quad (4)$$

When the total magnetic energy is calculated for both the force-free and potential field,  $E_{FF}$  and  $E_{PF}$  respectively, the free magnetic energy can be estimated using

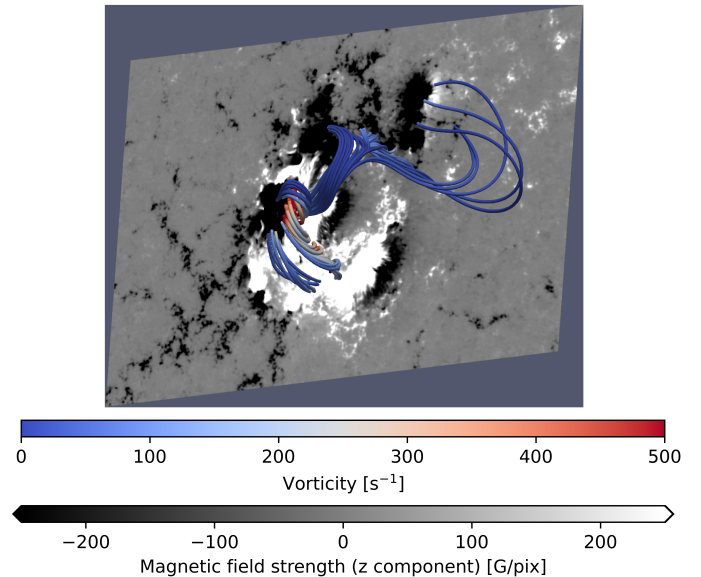
$$E_{free} = E_{FF} - E_{PF}. \quad (5)$$

To compute the potential field we use the approach by Sakurai (1982).

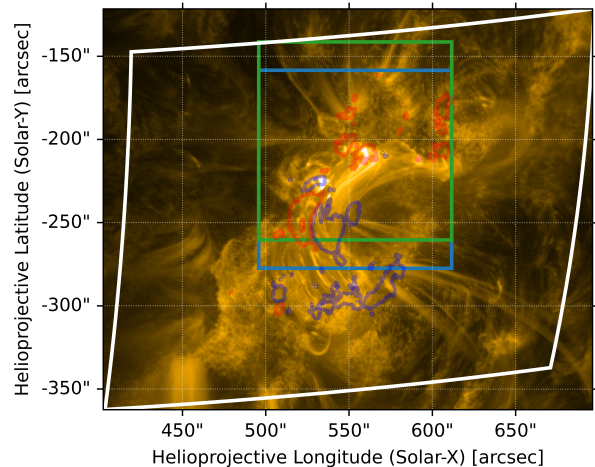
Furthermore, we calculate a column-integrated free magnetic energy, summed along the EIS line of sight, which allows the free magnetic energy to be spatially resolved for the active region in the same projection as EIS. This follows a similar procedure but integrates the total energies at an angle to the vertical to generate a two-dimensional map of the free magnetic energy.

### 3. RESULTS

Figure 3 shows the evolution of non-thermal velocity and free magnetic energy - at 3-minute and 12-minute cadence respectively - in active region NOAA 12673 over a 9-hour period encompassing two X-class flares. The



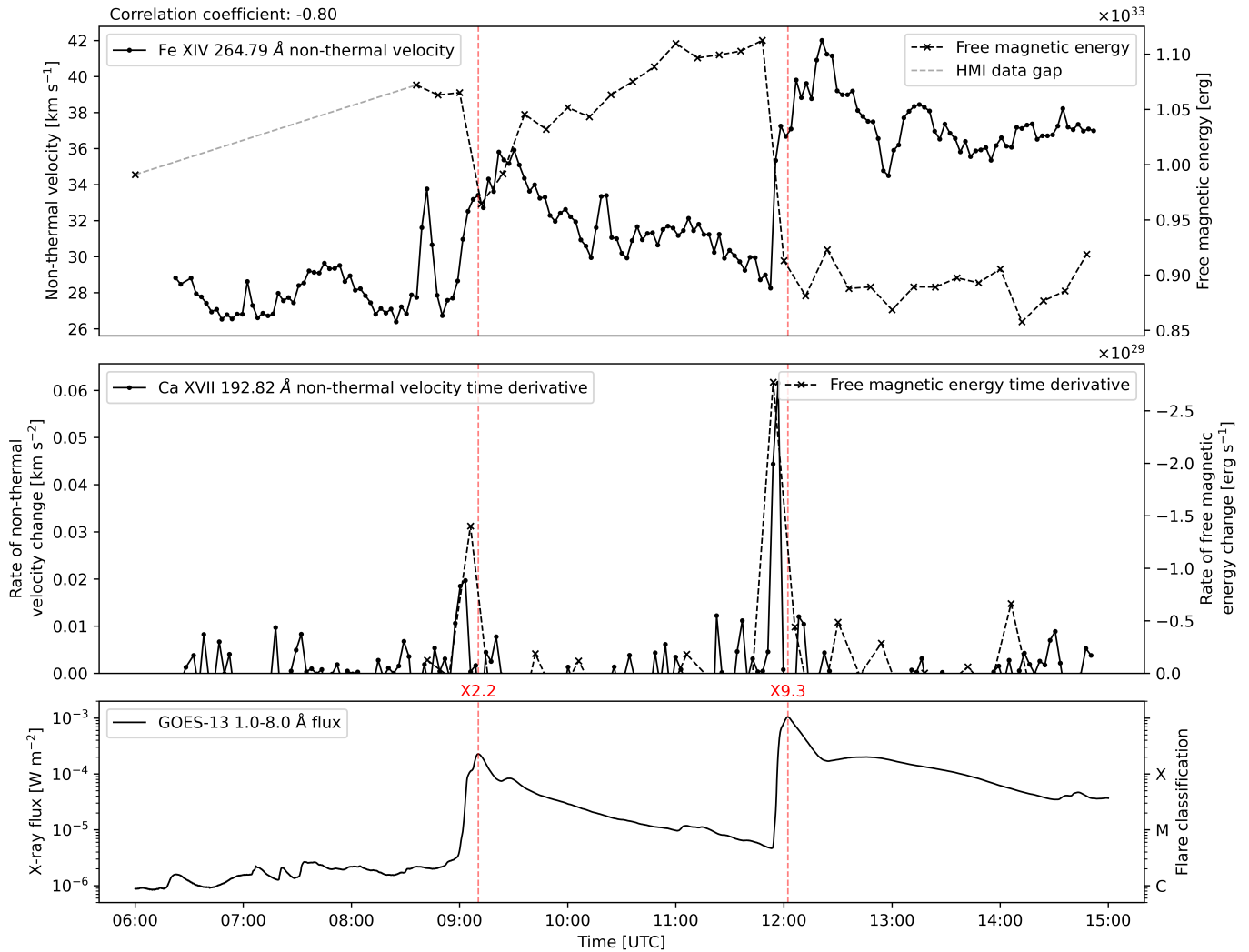
(a) Selected magnetic field lines as computed by the NLFFF modelling. The z component of the magnetic field is shown at the bottom of the extrapolation.



(b) AIA  $171 \text{ \AA}$  with overplotted contours of the photospheric negative (red) and positive (dark blue) magnetic field at  $-750 \text{ G}$  and  $750 \text{ G}$  respectively. Also shown is the region of SHARP 7115 used for NLFFF extrapolations (white) and the EIS field of view for the Fe XIV  $264.79 \text{ \AA}$  and Fe XIV  $274.20 \text{ \AA}$  emission lines (green) and the Ca XVII  $192.82 \text{ \AA}$  emission line (light blue).

**Figure 2.** Cospacial maps of the NLFFF modelling and the coronal EUV emission showing the agreement of the magnetic structures resolved by the NLFFF extrapolation and the structures visible in the EUV. These plots are of the active region as observed at 11:36 UTC, just before the onset of the X9.3 flare.

times and classifications of the two X-class flares that occurred during this time period are also identified using the peak soft X-ray flux data from GOES-13, these being confined X2.2 and eruptive X9.3 flares at 09:10:25 UTC



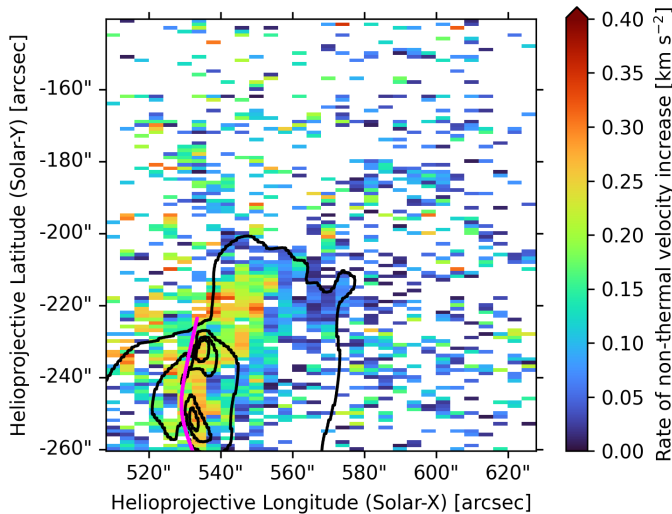
**Figure 3.** Top panel: The non-thermal velocity time series from 6 September 2017 as derived from the Fe XIV 264.79 Å emission line widths as observed by Hinode/EIS (solid line; left axis). Also plotted is the free magnetic energy as estimated using potential and non-potential field modelling based on observations performed by SDO/HMI for SHARP 7115 (dashed line; right axis). An HMI data gap at the beginning of the window is highlighted by a grey line. Middle panel: The non-thermal velocity time derivative for the Ca XVII 192.82 Å emission line as observed by EIS (solid line; left axis) is plotted alongside the free magnetic energy time derivative, plotted flipped so that negative values are shown at the top (dashed line; right axis). As discussed in the text, the calculated Ca XVII 192.82 Å is a lower estimate. Bottom panel: The soft X-ray flux as observed by the GOES-13 spacecraft between 1.0 Å and 8.0 Å is plotted. A red vertical line is added across all the panels at the time of peak soft X-ray flux to show the flaring times and annotated to identify the flare classification.

and 12:02:13 UTC respectively. The magnitudes of magnetic energy calculated by our study are in agreement with those reported by Fleishman et al. (2020). The Pearson product-moment correlation coefficient was calculated for each time series pair (Bravais 1846), and found to be  $-0.80$  between the Fe XIV 264.79 Å non-thermal velocity and free magnetic energy, as seen in the top panel of Figure 3.

As seen in the top panel of Figure 3, the level of free magnetic energy in the extrapolated field drops during flaring. This drop is unresolved temporally and takes place within one data point. At the same time, the

observed non-thermal velocity rises during flaring, this time being temporally resolved for the first flare and partially temporally resolved for the second. This respective behaviour is strongly negatively correlated. The Fe XIV 264.79 Å is shown as it provided a representative time series for the entire 9-hour window, not just during flaring. The Fe XIV 274.20 Å emission line results in a similar time series with a slightly stronger negative correlation.

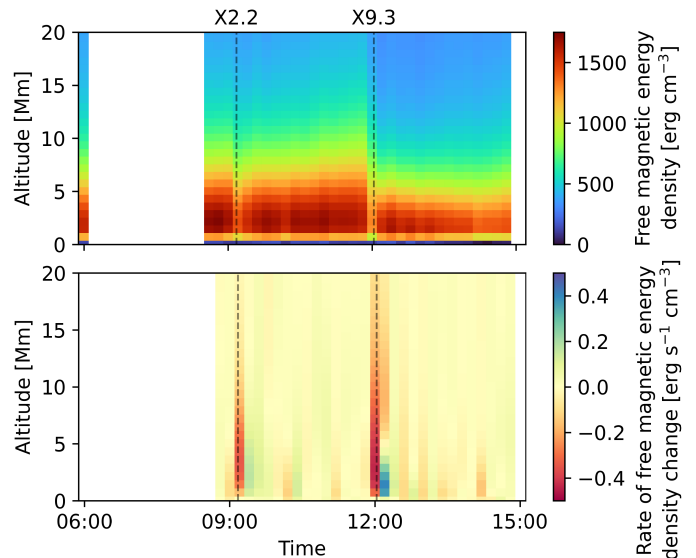
The middle panel of Figure 3 reveals several key features. Firstly, it establishes the temporal coincidence of the increase in non-thermal velocity, the decrease in free



**Figure 4.** Spatially-resolved rate of non-thermal velocity increase in active region NOAA 12673 on 6 September 2017 between 11:52 and 11:55 UTC as calculated using the Fe XIV 264.79 Å emission line. Overplotted is the rate of free magnetic energy decrease between 11:48 and 12:00 UTC, with contours between  $-5 \times 10^5 \text{ erg s}^{-1} \text{ cm}^{-2}$  and  $-1 \times 10^5 \text{ erg s}^{-1} \text{ cm}^{-2}$ . The polarity inversion line is illustrated in pink. White pixels represent those either showing a non-thermal velocity decrease, or where the fitting of spectral data was not possible.

magnetic energy, and the peak in soft X-ray flux. The Ca XVII 192.82 Å emission line is shown because it is particularly responsive to large flares. Although more noisy, a similar proportional trend is observed in the Fe XIV 264.79 Å and Fe XIV 274.20 Å emission lines. Secondly, these time series exhibit a proportional response to flaring. The ratio of the peak rate of free magnetic energy decrease to non-thermal velocity increase (Ca XVII 192.82 Å) is around  $3.5 \times 10^{29} \text{ erg s cm}^{-1}$  for both flares. This proportional behaviour is not unique to Ca XVII and is also evident in the other Fe XIV lines we studied. These time series are generated using the entire field of view of EIS and the entire NLFFF simulation volume. When considering only the free magnetic energy within the EIS field of view, a similar correlation is present.

After identifying the time period of interest for the X9.3 flare, we spatially resolved the respective increases and decreases in non-thermal velocity and free magnetic energy. Figure 4 shows the spatially-resolved time derivative of non-thermal velocity between 11:52 and 11:55 UTC and the spatially-resolved time derivative of free magnetic energy between 11:48 and 12:00 UTC. This respective increase and decrease are positively correlated.

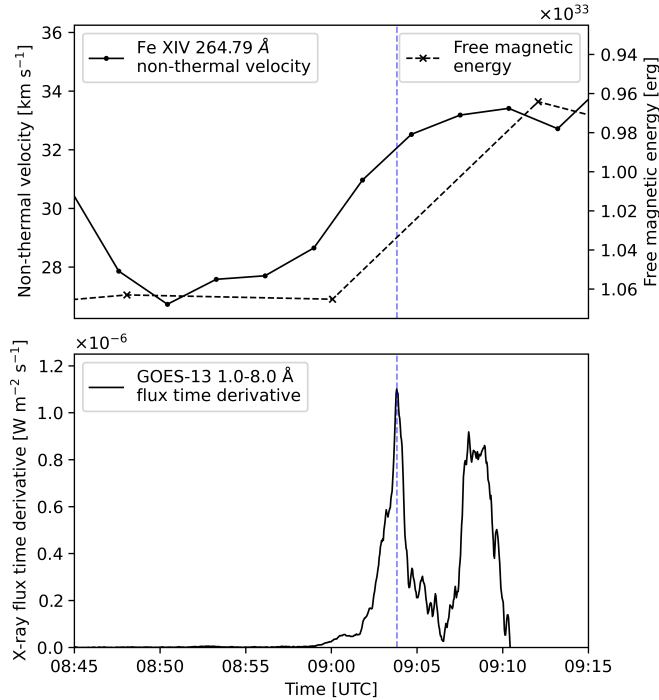


**Figure 5.** Free magnetic energy density distribution in height (top) and its time derivative (bottom), with the flare times and classifications identified, for 6 September 2017

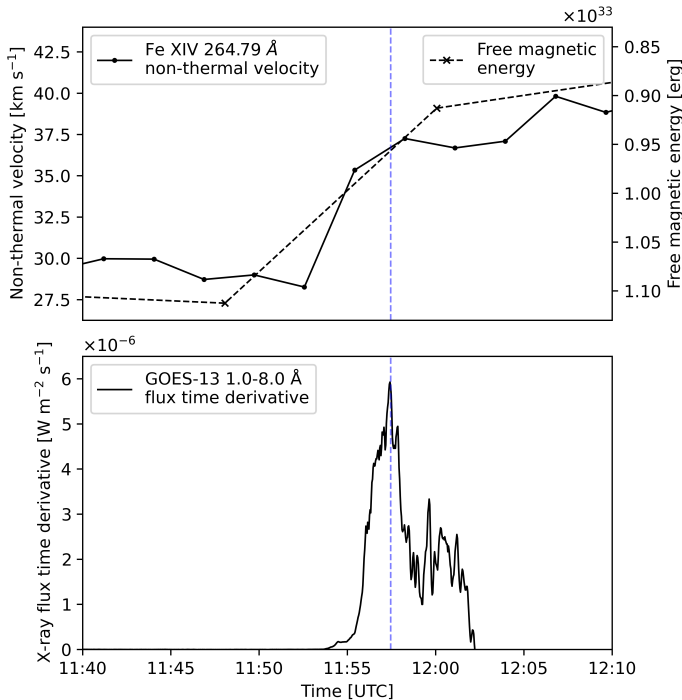
Additionally, we calculated the free magnetic energy density distribution in height, and its time derivative, to identify the altitudes at which changes in the free magnetic energy occurred. This is shown in Figure 5. The building of the pre-eruptive structure is known to happen prior to an eruptive event and rises before the main eruption (Zhang et al. 2001; Sterling & Moore 2005). While the HMI data gap means no information can be presented prior to the confined X2.2 flare, prior to the eruptive X9.3 flare, the free magnetic energy is seen to increase in magnitude and altitude. This coincides with observations of the corona made at 193 Å using AIA, which also show a slow-rising structure during this period. The time derivative plot shows the peak rate of free magnetic energy decrease to be at around 5 Mm in altitude.

In order to better understand the chromospheric response during the observed flares, and given the absence of direct hard X-ray data covering both flares, we employ the Neupert effect, which posits a correlation between the time-integrated hard X-ray emission and the soft X-ray emission (Dennis & Zarro 1993; Veronig et al. 2002), as a proxy to investigate the potential role of chromospheric evaporation in driving non-thermal velocities. Figure 6 presents the temporal evolution of the non-thermal velocity, alongside the time derivative of the 1–8 Å soft X-ray flux as observed by the GOES-13 spacecraft.

#### 4. DISCUSSION



(a) Non-thermal velocity, free magnetic energy, and soft X-ray flux time derivative for the X2.2 flare.



(b) Non-thermal velocity, free magnetic energy, and soft X-ray flux time derivative for the X9.3 flare.

**Figure 6.** Top panels: The Fe XIV 264.79 Å non-thermal velocity (solid line; left axis) and free magnetic energy plotted flipped with lower values at the top (dashed line; right axis). Bottom panels: The time derivative of the GOES soft X-ray flux. A blue vertical line indicates the peak time of the soft X-ray flux time derivative.

The primary result of this study is the strong temporal and spatial coupling between increases in non-thermal velocity and decreases in free magnetic energy during the two large flares considered. These changes occur within minutes of the rise and peak in soft X-ray flux, indicative of the solar flare energy release process: a rapid conversion of magnetic energy into kinetic and thermal energy of the plasma, in line with the standard flare model. This behaviour is also broadly in agreement with the energy budget of flares described by [Aschwanden et al. \(2017\)](#).

As discussed in [Polito et al. \(2019\)](#) and references found herein, the possible causes of excess line broadening during solar flares include: the superposition of unresolved flows with various Doppler-shifted components; Alfvén wave propagation accelerating ions perpendicular to the magnetic field; departures from ionisation equilibrium as the result of high temperatures; isotropic turbulence.

#### 4.1. Superposition of unresolved flows

Using modelling of superposed Doppler-shifted flows, [Polito et al. \(2019\)](#) concluded that this mechanism fails to explain the broadening observed by IRIS (Interface Region Imaging Spectrometer; [De Pontieu et al. 2014](#)) during an X-class flare. Such flows would be produced as the result of chromospheric evaporation, a secondary response to the primary energy release, and typically on timescales of approximately 100 seconds ([Ning 2012](#)). The close timing of free magnetic energy decrease and non-thermal velocity increase found in our study is in broad agreement with these findings, although our limited observational cadence, 12 minutes for the former and 3 minutes for the latter, makes it difficult to provide conclusive support. The Neupert effect suggests that the non-thermal electron bombardment, typically observed in hard X-rays, heats the chromosphere, leading to chromospheric evaporation filling the coronal loops with hot plasma which results in the enhanced soft X-ray emission. Therefore, the time derivative of the soft X-ray flux can serve as an indicator of the non-thermal electron precipitation in the absence of hard X-ray data. In both the X2.2 and X9.3 flares, the peak in the soft X-ray flux derivative, indicative of the maximum rate of chromospheric evaporation, is seen in [Figure 6](#) to occur after observed increases in non-thermal velocity. We, therefore, conclude that the increase in the observed non-thermal velocity is more closely connected to the initial energy release in the corona than to the response to energy deposition in the chromosphere.

#### 4.2. Alfvén wave propagation

The spatial, temporal and spectral resolution of the EIS observations in our study make it challenging to draw any conclusions about the presence of Alfvén waves as the main cause of line broadening. However, we note that [De Pontieu et al. \(2022\)](#) demonstrate that the inclusion of Alfvén waves in flare simulations can result in increased line broadening of magnitudes similar to those measured in this work and on similar timescales.

#### 4.3. Departures from ionisation equilibrium

Using EIS observations of highly ionised Fe lines in flares, [Kawate et al. \(2016\)](#) found some evidence of departures from ionisation equilibrium in a small number of pixels (approximately 1%), from which they concluded that equilibrium holds in most cases for EIS exposures. While our observations include lines formed at lower temperatures than those studied by [Kawate et al. \(2016\)](#), and while departures cannot be completely ruled out, we consider non-thermal broadening from this effect unlikely.

#### 4.4. Isotropic turbulence

The question of the origin and presence of turbulence is closely linked to the conditions that are favourable to the onset and evolution of magnetic reconnection and/or instability, and the release of free magnetic energy. However, which comes first remains a major open question. [French et al. \(2021\)](#) found evidence supporting the development of the tearing mode instability prior to the increase in excess line broadening followed by a rapid increase in line broadening and evolution of the energy spectrum to a turbulence dominated regime, something supported by simulations ([Dong et al. 2018](#); [Tenerani & Velli 2020](#)). For the events studied here, we observe a gradual increase in line broadening followed by a rapid increase coincident with the drop in free magnetic energy for the first X-class flare, and a coincident increase in line broadening and a decrease in free magnetic energy for the second. With the caveat that our temporal resolution is low compared to typical impulsive phase timescales, we suggest that the close inverse relationship found in our work is consistent with the scenario of a turbulent cascade in response to free magnetic energy release.

[Harra et al. \(2013\)](#) observed differences between eruptive and confined events in the pre-flare enhancement

of non-thermal velocity, with a confined event showing enhancement only in the flaring region and eruptive events additionally showing enhancement at footpoints and close to or above the loop regions. The height of the behaviour we observed in the plasma is difficult to ascertain relative to the height of the behaviour we observed in the magnetic field given only line of sight observations near to vertically above the flare were made by EIS. However, we find our observation of a concentrated non-thermal velocity enhancement in the eruptive flare, in the same region as a free magnetic energy drop, to be broadly consistent with the findings of [Harra et al. \(2013\)](#).

#### 4.5. Conclusions

In conclusion, our study reveals a strong temporal and spatial correlation between increases in non-thermal velocity and decreases in free magnetic energy during solar flares, consistent with the standard flare model of reconnection-driven energy conversion. Our findings contribute to the understanding of the complex interplay between magnetic fields and plasma dynamics in solar flares, and are consistent with the suggestion that Alfvén wave propagation and isotropic turbulence are more likely to be responsible for non-thermal line broadening.

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